

1. What is the potential energy of a 25kg block which is 15m above the ground?

$$E_p = mgh = 25 \text{ kg} \times 9.8 \text{ m/s}^2 \times 15 \text{ m}$$

$$= 3675 \text{ J} \approx \textcircled{3700 \text{ J}}$$

2. How much work must be done to lift a 25kg block to a height of 15m above the ground?

$$W = Fd$$



$$F = mg$$

$$= 25 \times 9.8$$

$$= 245$$

$$W = 245 \times 15 = 3675 \text{ J}$$

This is really the same question

$$\textcircled{W = 3700 \text{ J}}$$

3. What is the kinetic energy of a 25 kg block which is moving at 15 m/s?

$$E_k = \frac{1}{2} mv^2 = \frac{1}{2} (25) (15)^2$$

$$= \textcircled{2800 \text{ J}}$$

4. ~~What is the kinetic energy of an 85 kg person who is running at 5.3 m/s?~~

How fast is someone running if they are 85kg and have 1100J of energy?

$$E_k = \frac{1}{2} mv^2$$

$$v = \sqrt{\frac{2E_k}{m}} = \sqrt{\frac{2(1100)}{85}} = \textcircled{5.1 \text{ m/s}}$$

- 850 kg  
 5. A car increases its velocity from rest to 25.0 m/s.  
 a. What is the initial kinetic energy of the car?

0 J

- b. What is the final kinetic energy of the car?

$$E_k = \frac{1}{2}mv^2 = \frac{1}{2}(850)(25)^2$$

$$= 265625 \text{ J} = 2.7 \times 10^5 \text{ J}$$

- c. What is  $\Delta E_k$ ?

# Final - Initial

$$2.7 \times 10^5 \text{ J} - 0 \text{ J} = 2.7 \times 10^5 \text{ J}$$

- 850 kg  
 6. A car increases its velocity from 25.0 m/s to 50.0 m/s.

- a. What is the initial kinetic energy of the car?

$$\frac{1}{2}(850)(25)^2 = 2.7 \times 10^5 \text{ J}$$

- b. What is the final kinetic energy of the car?

$$\frac{1}{2}(850)(50)^2 = 1.1 \times 10^6 \text{ J}$$

$$= 1062500 \text{ J}$$

- c. What is  $\Delta E_k$ ?

$$\text{Final} - \text{Initial} = 8.0 \times 10^5 \text{ J}$$

$$1062500 \text{ J} - 265625 \text{ J}$$

- d. It takes more energy to speed up from 25 m/s to 50 m/s.

7. A 25 kg block is dropped from a height of 5.0m. We want to determine how fast it will be moving when it hits the ground.

- a. Method 1: Use kinematics to determine how fast it will be moving when it hits the ground.

Use  $v_f^2 = v_o^2 + 2ad$

$$v_f = 9.9 \text{ m/s}$$

$$d = -5.0 \text{ m}$$

$$v_o = 0 \text{ m/s}$$

$$a = -9.8 \text{ m/s}^2$$

$$v_f = ?$$

- b. Method 2: Use conservation of energy (kinetic energy at the end will equal potential energy at the start) to determine how fast it will be moving when it hits the ground.

$$\text{Potential energy} = mgh$$

$$= 25 \times 9.8 \times 5.0$$

$$= 1225 \text{ J}$$

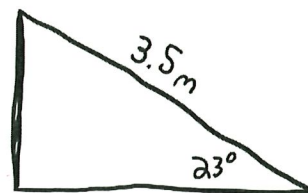
$$\text{Kinetic energy} = \frac{1}{2}mv^2$$

$$v = \sqrt{\frac{2 E_k}{m}}$$

$$= \sqrt{\frac{2(1225)}{25}}$$

$$= 9.9 \text{ m/s}$$

8. A 34 kg block is pushed up a 3.5m long,  $23^\circ$  frictionless incline at a constant velocity. We want to know how much work is needed to push the block up the incline.



- a. Method 1: Determine the force needed to push the block at a constant velocity (this will be equal to  $F_{g\parallel}$ ) and use  $W = Fd$  to determine the amount of work needed to push the block 3.5m.

$$F_{g\parallel} = \sin 23 \times 34 \times 9.8 = 130.19 \text{ N}$$

$$W = Fd = 130.19 \times 3.5 = 455.67 \text{ J}$$

$$\approx \textcircled{460 \text{ J}}$$

- b. Method 2: Use trigonometry to determine how high the block will be off the ground at the end of the 3.5m incline then use  $E_p = mgh$  to determine the work needed to push the block to that height.



$$\sin 23 = \frac{h}{3.5}$$

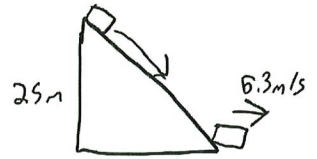
$$\sin 23 \times 3.5 = 1.3676 \text{ m}$$

$$E_p = 34 \times 9.8 \times 1.3676 \text{ m}$$

$$= 455.67 \text{ J}$$

$$\approx \textcircled{460 \text{ J}}$$

9. A 56kg sled, initially at rest on a 25m high hill, slides down. At the bottom of the hill the sled is moving at 6.3 m/s.



- a. What was the potential energy of the sled at the top of the hill?

$$E_p = mgh = 56 \times 9.8 \times 25 = 13720 \text{ J}$$

- b. What was the potential energy at the bottom of the hill?

0

- c. What was the change in potential energy?

$$-13720 \text{ J}$$

- d. What was the kinetic energy of the sled at the top of the hill?

0

- e. What was the kinetic energy at the bottom of the hill?

$$E_k = \frac{1}{2}mv^2 = \frac{1}{2}(56)(6.3)^2 = 1111.32$$

- f. What was the change in kinetic energy?

$$+1111.32 \text{ J}$$

- g. Determine how much heat was generated by friction. (This will be all the potential energy at the start which didn't get transformed into kinetic energy).

$$13720 - 1111 = 12609$$

$$\approx 13000 \text{ J}$$

$$\approx 1.3 \times 10^4 \text{ J}$$

10. A kid on a crazy carpet slides down a 15.0m tall hill. If the total mass of the kid and the carpet is 19kg and they are moving at 12.0 m/s at the bottom of the hill how much heat was generated?

$$E_p \text{ at start} = mgh = 19 \times 9.8 \times 15 \\ = 2793$$

$$E_k \text{ at end} = \frac{1}{2}mv^2 = \frac{1}{2}(19)(12)^2 \\ = 1368$$

$$\text{Difference: } 2793 - 1368 = 1425$$

$\approx$  1400 J of heat was generated

11. A 0.750 kilogram rubber ball is dropped from a height of 1.50 m. If 2.0 J of energy is lost during the interaction of the ball with the floor, how high will the ball bounce up from the floor?

$$E_p \text{ at start} = 0.75 \times 9.8 \times 1.5 = 11.025 \text{ J}$$

$$E_p \text{ at end} = 11.025 - 2 = 9.025 \text{ J}$$

$$\frac{9.025}{9.8} = h \rightarrow \frac{9.025}{9.8} = h \rightarrow \frac{9.025}{9.8} = 0.92 \text{ m}$$

12. A 65 kg person is running along a gym floor with a speed of 3.5 m/s. She grabs on to a rope hanging from the ceiling of the gym and swings from the end of the rope.

- a. Determine the initial kinetic energy of the person.

$$E_k = \frac{1}{2}(65)(3.5)^2 = 398.125 \text{ J}$$

$$\approx 4.0 \times 10^2 \text{ J}$$

- b. Determine how high they will swing if all of their kinetic energy is converted into potential energy.

$$E_p = mgh \rightarrow h = \frac{E_p}{mg}$$

$$h = \frac{398.125}{65 \times 9.8}$$

$$= 0.625$$

$$\approx 0.63 \text{ m}$$

13. We wish to determine how far a 50.0 kg object can move along a surface with  $\mu=0.12$  at a constant rate using 500.0 J of energy.

- a. Determine the force of friction acting on the object using the formula  $F_{fric} = \mu F_N$

$$F_N = F_g = mg = 50 \times 9.8 = 490 \text{ N}$$

$$F_{fric} = \mu F_N = 0.12 \times 490 = 58.8 \text{ N}$$

- b. Solve for displacement using the formula  $W = Fd$ .

$$W = Fd \rightarrow d = \frac{W}{F} = \frac{500}{58.8} = 8.5 \text{ m}$$

14. A 12 kg object initially moving at 25 m/s is slowed by friction.  $\mu$  between the object and the floor is 0.46. We wish to determine how far it will travel before it stops without using kinematics.

- a. Determine the initial kinetic energy of the object.

$$E_k = \frac{1}{2}mv^2 = \frac{1}{2}(12)(25)^2$$

$$= 3750 \text{ J}$$

- b. Determine the force of friction acting on the object.

$$F_{fric} = 0.46 \times 12 \times 9.8 = 54.096 \text{ N}$$

- c. All of the initial kinetic energy from the object will be converted to heat by friction. Use  $W = Fd$  to determine how far the object will move before stopping.

$$d = \frac{W}{F} = \frac{3750}{54.096} = 69 \text{ m}$$